## 1MHz, Four Quadrant Analog Multiplier

The ICL8013 is a four quadrant analog multiplier whose output is proportional to the algebraic product of two input signals. Feedback around an internal op amp provides level shifting and can be used to generate division and square root functions. A simple arrangement of potentiometers may be used to trim gain accuracy, offset voltage and feedthrough performance. The high accuracy, wide bandwidth, and increased versatility of the ICL8013 make it ideal for all multiplier applications in control and instrumentation systems. Applications include RMS measuring equipment, frequency doublers, balanced modulators and demodulators, function generators, and voltage controlled amplifiers.

Part Number Information

| PART <br> NUMBER | MULTIPLI- <br> CATION <br> ERROR <br> (MAX) | TEMP. <br> RANGE (${ }^{\circ}$ C) |
| :---: | :---: | :---: | :---: | :---: |$\quad$ PKG | PKG. |
| :---: |
| NO. |$|$

## Features

- Accuracy . . . . . . . . . . . . . . . . . . . . . . . $\pm 1 \%$ ("B" Version)
- Input Voltage Range . . . . . . . . . . . . . . . . . . . . . . . $\pm 10 \mathrm{~V}$
- Bandwidth . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . 1 MHz
- Uses Standard $\pm 15 \mathrm{~V}$ Supplies
- Built-In Op Amp Provides Level Shifting, Division and Square Root Functions


## Pinot

ICL8013
(METAL CAN)
TOP VIEW


## Functional Diagram



## ICL8013

## Absolute Maximum Ratings

Supply Voltage.
. $\qquad$
Input Voltages ( $\mathrm{X}_{\mathrm{IN}}, \mathrm{Y}_{\mathrm{IN}}, \mathrm{Z}_{\mathrm{IN}}, \mathrm{X}_{\mathrm{OS}}, \mathrm{Y}_{\mathrm{OS}}, \mathrm{Z}_{\mathrm{OS}}$ ). $\qquad$ $V_{\text {SUPPLY }}$

## Operating Conditions

Temperature Range
ICL8013XC. . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . $0^{\circ} \mathrm{C}$ to $70^{\circ} \mathrm{C}$

CAUTION: Stresses above those listed in "Absolute Maximum Ratings" may cause permanent damage to the device. This is a stress only rating and operation of the device at these or any other conditions above those indicated in the operational sections of this specification is not implied.

NOTE:

1. $\theta_{\mathrm{JA}}$ is measured with the component mounted on an evaluation PC board in free air.

Electrical Specifications $\mathrm{T}_{\mathrm{A}}=25^{\circ} \mathrm{C}, \mathrm{V}_{\text {SUPPLY }}= \pm 15 \mathrm{~V}$, Gain and Offset Potentiometers Externally Trimmed, Unless Otherwise Specified

| PARAMETER | TEST CONDITIONS | ICL8013B |  |  | ICL8013C |  |  | UNITS |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | MIN | TYP | MAX | MIN | TYP | MAX |  |
| Multiplier Function |  | - | $\frac{\mathrm{XY}}{10}$ | - | - | $\frac{X Y}{10}$ | - |  |
| Multiplication Error | $\begin{aligned} & -10<X<10 \\ & -10<Y<10 \end{aligned}$ | - | - | 1.0 | - | - | 2.0 | \% Full Scale |
| Divider Function |  | - | $\frac{10 Z}{X}$ | - | - | $\frac{10 Z}{x}$ | - |  |
| Division Error | $X=-10$ | - | 0.3 | - | - | 0.3 | - | \% Full Scale |
|  | $\mathrm{X}=-1$ | - | 1.5 | - | - | 1.5 | - | \% Full Scale |
| Feedthrough | $\mathrm{X}=0, \mathrm{Y}= \pm 10 \mathrm{~V}$ | - | - | 100 | - | - | 200 | mV |
|  | $Y=0, X= \pm 10 \mathrm{~V}$ | - | - | 100 | - | - | 150 | mV |
| Non-Linearity X Input | $\begin{aligned} & X=20 V_{P-P} \\ & Y= \pm 10 V_{D C} \end{aligned}$ | - | $\pm 0.5$ | - | - | $\pm 0.8$ | - | \% |
| Y Input | $\begin{aligned} & \mathrm{Y}=20 \mathrm{~V}_{\mathrm{P}-\mathrm{P}} \\ & \mathrm{X}= \pm 10 \mathrm{~V}_{\mathrm{DC}} \end{aligned}$ | - | $\pm 0.2$ | - | - | $\pm 0.3$ | - | \% |
| Frequency Response Small Signal Bandwidth (-3dB) |  | - | 1.0 | - | - | 1.0 | - | MHz |
| Full Power Bandwidth |  | - | 750 | - | - | 750 | - | kHz |
| Slew Rate |  | - | 45 | - | - | 45 | - | V/us |
| 1\% Amplitude Error |  | - | 75 | - | - | 75 | - | kHz |
| 1\% Vector Error (0.5 ${ }^{\circ}$ Phase Shift) |  | - | 5 | - | - | 5 | - | kHz |
| Settling Time (to $\pm 2 \%$ of Final Value) | $\mathrm{V}_{\text {IN }}= \pm 10 \mathrm{~V}$ | - | 1 | - | - | 1 | - | $\mu \mathrm{s}$ |
| Overload Recovery (to $\pm 2 \%$ of Final Value) | $\mathrm{V}_{\text {IN }}= \pm 10 \mathrm{~V}$ | - | 1 | - | - | 1 | - | $\mu \mathrm{s}$ |
| Output Noise | 5 Hz to 10 kHz | - | 0.6 | - | - | 0.6 | - | mV RMS |
|  | 5 Hz to 5 MHz | - | 3 | - | - | 3 | - | mV RMS |
| Input Resistance X Input | $\mathrm{V}_{\mathrm{IN}}=0 \mathrm{~V}$ | - | 10 | - | - | 10 | - | $\mathrm{M} \Omega$ |
| Y Input |  | - | 6 | - | - | 6 | - | $\mathrm{M} \Omega$ |
| Z Input |  | - | 36 | - | - | 36 | - | $\mathrm{k} \Omega$ |
| Input Bias Current X or Y Input | $\mathrm{V}_{\text {IN }}=0 \mathrm{~V}$ | - | - | 7.5 | - | - | 10 | $\mu \mathrm{A}$ |
| Z Input |  | - | 25 | - | - | 25 | - | $\mu \mathrm{A}$ |

## Electrical Specifications $\mathrm{T}_{\mathrm{A}}=25^{\circ} \mathrm{C}, \mathrm{V}_{\text {SUPPLY }}= \pm 15 \mathrm{~V}$, Gain and Offset Potentiometers Externally Trimmed, Unless Otherwise Specified (Continued)

| PARAMETER | TEST CONDITIONS | ICL8013B |  |  | ICL8013C |  |  | UNITS |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | MIN | TYP | MAX | MIN | TYP | MAX |  |
| Power Supply Variation Multiplication Error |  | - | 0.2 | - | - | 0.2 | - | \%/\% |
| Output Offset |  | - | - | 75 | - | - | 100 | $\mathrm{mV} / \mathrm{V}$ |
| Scale Factor |  | - | 0.1 | - | - | 0.1 | - | \%/\% |
| Quiescent Current |  | - | 3.5 | 6.0 | - | 3.5 | 6.0 | mA |

THE FOLLOWING SPECIFICATIONS APPLY OVER THE OPERATING TEMPERATURE RANGES

| Multiplication Error | $\begin{aligned} & -10 \mathrm{~V}<\mathrm{X}_{\text {IN }}<10 \mathrm{~V}, \\ & -10 \mathrm{~V}<\mathrm{Y}_{\text {IN }}<10 \mathrm{~V} \end{aligned}$ | - | 2 | - | - | 3 | - | \% Full Scale |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Average Temp. Coefficients Accuracy |  | - | 0.06 | - | - | 0.06 | - | \%/ ${ }^{\circ} \mathrm{C}$ |
| Output Offset |  | - | 0.2 | - | - | 0.2 | - | $\mathrm{mV} /{ }^{\circ} \mathrm{C}$ |
| Scale Factor |  | - | 0.04 | - | - | 0.04 | - | \%/ ${ }^{\circ} \mathrm{C}$ |
| Input Bias Current X or Y Input | $\mathrm{V}_{\mathrm{IN}}=0 \mathrm{~V}$ | - | - | 5 | - | - | 10 | $\mu \mathrm{A}$ |
| Z Input |  | - | - | 25 | - | - | 35 | $\mu \mathrm{A}$ |
| Input Voltage (X, Y, or Z) |  | - | - | $\pm 10$ | - | - | $\pm 10$ | V |
| Output Voltage Swing | $\begin{aligned} & \mathrm{R}_{\mathrm{L}} \geq 2 \mathrm{k} \Omega \\ & \mathrm{C}_{\mathrm{L}}<1000 \mathrm{pF} \end{aligned}$ | - | $\pm 10$ | - | - | $\pm 10$ | - | V |

## Schematic Diagram



## Application Information

## Detailed Circuit Description

The fundamental element of the ICL8013 multiplier is the bipolar differential amplifier of Figure 1.


FIGURE 1. DIFFERENTIAL AMPLIFIER

The small signal differential voltage gain of this circuit is given by:
$A_{V}=\frac{V_{\text {OUT }}}{V_{I N}}=\frac{R_{L}}{r_{E}}$
Substituting $r_{E}=\frac{1}{g_{M}}=\frac{k T}{q^{l_{E}}}$
$V_{\text {OUT }}=V_{\text {IN }}\left(\frac{R_{L}}{r_{E}}\right)=V_{\text {IN }} \times \frac{\text { qI }_{E} R_{L}}{k T}$
The output voltage is thus proportional to the product of the input voltage $\mathrm{V}_{\mathrm{IN}}$ and the emitter current $\mathrm{I}_{\mathrm{E}}$. In the simple transconductance multiplier of Figure 2, a current source comprising $Q_{3}, D_{1}$, and $R_{Y}$ is used. If $V_{Y}$ is large compared with the drop across $D_{1}$, then

$$
\begin{aligned}
& \mathrm{I}_{\mathrm{D}} \approx \frac{\mathrm{~V}_{Y}}{R_{Y}}=2 \mathrm{I}_{\mathrm{E}} \text { and } \\
& \mathrm{V}_{\text {OUT }}=\frac{q R_{L}}{\mathrm{kTR}_{Y}}\left(\mathrm{~V}_{X} \times \mathrm{V}_{Y}\right)
\end{aligned}
$$



FIGURE 2. TRANSCONDUCTANCE MULTIPLIER

There are several difficulties with this simple modulator:

1. $V_{Y}$ must be positive and greater than $V_{D}$.
2. Some portion of the signal at $\mathrm{V}_{\mathrm{X}}$ will appear at the output unless $\mathrm{I}_{\mathrm{E}}=0$.
3. $V_{X}$ must be a small signal for the differential pair to be linear.
4. The output voltage is not centered around ground.

The first problem relates to the method of converting the $\mathrm{V}_{\mathrm{Y}}$ voltage to a current to vary the gain of the $\mathrm{V}_{\mathrm{X}}$ differential pair. A better method, Figure 3, uses another differential pair but with considerable emitter degeneration. In this circuit the differential input voltage appears across the common emitter resistor, producing a current which adds or subtracts from the quiescent current in either collector. This type of voltage to current converter handles signals from 0 V to $\pm 10 \mathrm{~V}$ with excellent linearity.


FIGURE 3. Voltage to current converter
The second problem is called feedthrough; i.e., the product of zero and some finite Input signal does not produce zero output voltage. The circuit whose operation is illustrated by Figures $4 \mathrm{~A}, 4 \mathrm{~B}$, and 4 C overcomes this problem and forms the heart of many multiplier circuits in use today.

This circuit is basically two matched differential pairs with cross coupled collectors. Consider the case shown in Figure 4A of exactly equal current sources basing the two pairs. With a small positive signal at $V_{I N}$, the collector current of $Q_{1}$ and $Q_{4}$ will increase but the collector currents of $Q_{2}$ and $Q_{3}$ will decrease by the same amount. Since the collectors are cross coupled the current through the load resistors remains unchanged and independent of the $\mathrm{V}_{\mathrm{IN}}$ input voltage.

In Figure 4B, notice that with $\mathrm{V}_{\mathrm{IN}}=0$ any variation in the ratio of biasing current sources will produce a common mode voltage across the load resistors. The differential output voltage will remain zero. In Figure 4C we apply a differential input voltage with unbalanced current sources. If $\mathrm{I}_{\mathrm{E} 1}$ is twice $I_{E 2}$ the gain of differential pair $Q_{1}$ and $Q_{2}$ is twice the gain of pair $Q_{3}$ and $Q_{4}$. Therefore, the change in cross coupled collector currents will be unequal and a differential output voltage will result. By replacing the separate biasing current sources with the voltage to current converter of Figure 3 we have a balanced multiplier circuit capable of four quadrant operation (Figure 5).


FIGURE 4A. INPUT SIGNAL WITH BALANCED CURRENT SOURCES $\Delta V_{\text {OUT }}=0 \mathrm{~V}$


FIGURE 4B. NO INPUT SIGNAL WITH UNBALANCED CURRENT SOURCES $\triangle V_{\text {OUT }}=0 V$


FIGURE 4C. INPUT SIGNAL WITH UNBALANCED CURRENT SOURCES, DIFFERENTIAL OUTPUT VOLTAGE

This circuit of Figure 5 still has the problem that the input voltage $\mathrm{V}_{\mathrm{IN}}$ must be small to keep the differential amplifier in the linear region. To be able to handle large signals, we need an amplitude compression circuit.


FIGURE 5. TYPICAL FOUR QUADRANT MULTIPLIERMODULATOR

Figure 2 showed a current source formed by relying on the matching characteristics of a diode and the emitter base junction of a transistor. Extension of this idea to a differential circuit is shown in Figure 6A. In a differential pair, the input voltage splits the biasing current in a logarithmic ratio. (The usual assumption of linearity is useful only for small signals.) Since the input to the differential pair in Figure 6A is the difference in voltage across the two diodes, which in turn is proportional to the log of the ratio of drive currents, it follows that the ratio of diode currents and the ratio of collector currents are linearly related and independent of amplitude. If we combine this circuit with the voltage to current converter of Figure 3, we have Figure 6B. The output of the differential amplifier is now proportional to the input voltage over a large dynamic range, thereby improving linearity while minimizing drift and noise factors.

The complete schematic is shown after the Electrical Specifications Table. The differential pair $Q_{3}$ and $Q_{4}$ form a voltage to current converter whose output is compressed in collector diodes $Q_{1}$ and $Q_{2}$. These diodes drive the balanced cross-coupled differential amplifier $Q_{7} / Q_{8} Q_{14} / Q_{15}$. The gain of these amplifiers is modulated by the voltage to current converter $Q_{9}$ and $Q_{10}$. Transistors $Q_{5}, Q_{6}, Q_{11}$, and $Q_{12}$ are constant current sources which bias the voltage to current converter. The output amplifier comprises transistors $Q_{16}$ through $Q_{27}$.


FIGURE 6A. CURRENT GAIN CELL


FIGURE 6B. VOLTAGE GAIN WITH SIGNAL COMPRESSION

## Definition of Terms

Multiplication/Division Error: This is the basic accuracy specification. It includes terms due to linearity, gain, and offset errors, and is expressed as a percentage of the full scale output.

Feedthrough: With either input at zero, the output of an ideal multiplier should be zero regardless of the signal applied to the other input. The output seen in a non-ideal multiplier is known as the feedthrough.
Nonlinearity: The maximum deviation from the best straight line constructed through the output data, expressed as a percentage of full scale. One input is held constant and the other swept through it nominal range. The nonlinearity is the component of the total multiplication/division error which cannot be trimmed out.

## Typical Applications

## Multiplication

In the standard multiplier connection, the $Z$ terminal is connected to the op amp output. All of the modulator output current thus flows through the feedback resistor $\mathrm{R}_{27}$ and produces a proportional output voltage.

## MULTIPLIER TRIMMING PROCEDURE

1. Set $X_{I N}=Y_{I N}=0 V$ and adjust $Z_{O S}$ for zero Output.
2. Apply a $\pm 10 \mathrm{~V}$ low frequency $(\leq 100 \mathrm{~Hz})$ sweep (sine or triangle) to $\mathrm{Y}_{\mathrm{IN}}$ with $\mathrm{X}_{\mathrm{IN}}=0 \mathrm{~V}$, and adjust $\mathrm{X}_{\mathrm{OS}}$ for minimum output.
3. Apply the sweep signal of Step 2 to $X_{I N}$ with $Y_{I N}=0 V$ and adjust $Y_{O S}$ for minimum Output.
4. Readjust $Z_{O S}$ as in Step 1, if necessary.
5. With $X_{I N}=10.0 V_{D C}$ and the sweep signal of Step 2 applied to $Y_{I N}$, adjust the Gain potentiometer for Output $=Y_{I N}$. This is easily accomplished with a differential scope plug-in $(A+B)$ by inverting one signal and adjusting Gain control for (Output - $\mathrm{Y}_{\mathrm{IN}}$ ) = Zero.


FIGURE 7A. MULTIPLIER BLOCK DIAGRAM


FIGURE 7B. MULTIPLIER CIRCUIT CONNECTION

## Division

If the $Z$ terminal is used as an input, and the output of the op amp connected to the $Y$ input, the device functions as a divider. Since the input to the op amp is at virtual ground, and requires negligible bias current, the overall feedback forces the modulator output current to equal the current produced by $Z$.

Therefore $I_{O}=X_{I N} \cdot Y_{I N}=\frac{Z_{I N}}{R}=10 Z_{I N}$
Since $Y_{\text {IN }}=V_{\text {OUT }}, V_{\text {OUT }}=\frac{10 Z_{\text {IN }}}{X_{I N}}$
Note that when connected as a divider, the X input must be a negative voltage to maintain overall negative feedback.

## DIVIDER TRIMMING PROCEDURE

1. Set trimming potentiometers at mid-scale by adjusting voltage on pins 7, 9 and $10\left(\mathrm{X}_{\mathrm{OS}}, \mathrm{Y}_{\mathrm{OS}}, \mathrm{Z}_{\mathrm{OS}}\right)$ for 0 V .
2. With $Z_{I N}=0 V$, trim $Z_{O S}$ to hold the Output constant, as $\mathrm{X}_{\mathrm{IN}}$ is varied from -10 V through -1 V .
3. With $Z_{I N}=0 \mathrm{~V}$ and $X_{I N}=-10.0 \mathrm{~V}$ adjust $Y_{O S}$ for zero Output voltage.
4. With $Z_{I N}=X_{I N}$ (and/or $Z_{I N}=-X_{I N}$ ) adjust $X_{O S}$ for minimum worst case variation of Output, as $X_{I N}$ is varied from -10 V to -1 V .
5. Repeat Steps 2 and 3 if Step 4 required a large initial adjustment.
6. With $Z_{I N}=X_{I N}\left(\right.$ and $\left./ o r Z_{I N}=-X_{I N}\right)$ adjust the gain control until the output is the closest average around +10.0 V $\left(-10 \mathrm{~V}\right.$ for $\left.\mathrm{Z}_{I N}=-\mathrm{X}_{\mathrm{IN}}\right)$ as $\mathrm{X}_{\mathrm{IN}}$ is varied from -10 V to -3 V .


FIGURE 8A. DIVISION BLOCK DIAGRAM


FIGURE 8B. DIVISION CIRCUIT CONNECTION

## Squaring

The squaring function is achieved by simply multiplying with the two inputs tied together. The squaring circuit may also be used as the basis for a frequency doubler since $\cos ^{2} \omega t=1 / 2$ $(\cos 2 \omega t+1)$.


FIGURE 9A. SQUARER BLOCK DIAGRAM


FIGURE 9B. SQUARER CIRCUIT CONNECTION

## Square Root

Tying the $X$ and $Y$ inputs together and using overall feedback from the op amp results in the square root function.

The output of the modulator is again forced to equal the current produced by the Z input.
$\mathrm{I}_{\mathrm{O}}=\mathrm{X}_{\mathrm{IN}} \times \mathrm{Y}_{\text {IN }}=\left(-\mathrm{V}_{\text {OUT }}\right)^{2}=10 \mathrm{Z}_{\text {IN }}$
$\mathrm{V}_{\text {OUT }}=-\sqrt{10 Z_{\text {IN }}}$
The output is a negative voltage which maintains overall negative feedback. A diode in series with the op amp output prevents the latchup that would otherwise occur for negative input voltages.

## SQUARE ROOT TRIMMING PROCEDURE

1. Connect the ICL8013 in the Divider configuration.
2. Adjust $\mathrm{Z}_{\mathrm{OS}}, \mathrm{Y}_{\mathrm{OS}}, \mathrm{X}_{\mathrm{OS}}$, and Gain using Steps 1 through 6 of Divider Trimming Procedure.
3. Convert to the Square Root configuration by connecting $\mathrm{X}_{\mathrm{IN}}$ to the output and inserting a diode between Pin 4 and the output node.
4. With $Z_{I N}=O V$ adjust $Z_{O S}$ for zero output voltage.


FIGURE 10A. SQUARE ROOT BLOCK DIAGRAM


FIGURE 10B. ACTUAL CIRCUIT CONNECTION

## Variable Gain Amplifier

Most applications for the ICL8013 are straight forward variations of the simple arithmetic functions described above. Although the circuit description frequently disguises the fact, it has already been shown that the frequency doubler is nothing more than a squaring circuit. Similarly the variable gain amplifier is nothing more than a multiplier, with the input signal applied at the X input and the control voltage applied at the Y input.


FIGURE 11. VARIABLE GAIN AMPLIFIER

## Typical Performance Curves



FIGURE 13. FREQUENCY RESPONSE


FIGURE 12. POTENTIOMETERS FOR TRIMMING OFFSET AND FEEDTHROUGH


FIGURE 14. NONLINEARITY vs FREQUENCY


FIGURE 15. FEEDTHROUGH vs FREQUENCY

